$\Upsilon Z, A, C C Z'$,
$A \quad y\,3\; C\; A\; A$ ←
$\Upsilon Z, A, C \Upsilon' C$
$y\,3\; C\; A\; y' A$

$W\ X\ \Upsilon\ Z$ → $\bar{W}$, $X\ \Upsilon\ Z\ W$, $X\ \Upsilon$
$\bar{W}\ \bar{X}\ \bar{\Upsilon}\ \bar{Z}$ → $\bar{W}$, $\bar{X}\ \bar{\Upsilon}\ \bar{Z}\ \bar{W}$, $\bar{X}\ \bar{\Upsilon}$

Then split into cases

$\Upsilon Z, A, X' C C$,
$y\,3\; C, x' A A$

$W, X, \Upsilon, Z,$, $W_2 X_2 \Upsilon_2 Z_2$ → $X, \Upsilon, Z, W,$, $X_2 \Upsilon_2 Z_2 W_2$

$A, A A Z', A, X \Upsilon$

$A, A \Upsilon' A, A, X \Upsilon$
$A, X' A A, A, X \Upsilon Z$

Reduction definitive

Rules for $A, X \Upsilon Z,$

$A A Z'$ excludes $A Z' A$ + $Z' A X$
$A \Upsilon' A$ excludes $\Upsilon' A A$ + $A X \Upsilon$
$X' A A$ excludes $A A X$ + $A X \Upsilon$

Forwards
A in 1st position i.e. $A, A \Upsilon' Z', A$ →

Then $A \Upsilon' Z'$ excludes $\Upsilon' Z' A$

A in 2nd position $A, X' A Z', A, X$ →

$X' A Z'$ excludes $Z' A X$

A in 3rd position $A, X' \Upsilon' A, A, X \Upsilon$ →

$X' \Upsilon' A$ excludes $A X \Upsilon$

Backwards

C in 1st position $\Upsilon Z\ A, C \Upsilon' Z', A$
$y\,3\; C A, A$ ←

C_{3y}
$C \Upsilon' Z'$ excludes

C in 2nd position $Z, A, X' C Z', A$
$3\; C, x' A$ ←

$X' C Z'$ excludes $x' C_3$

$X' \Upsilon' C$ excludes $y' x' C$

C in Third position $A, X' \Upsilon' C, A$
$C\ x\ y\ A$

$C C Z'$ excludes C_{3y} + $A C_3$
$C \Upsilon' C$ excludes $y' A C$ + C_{3y}
$x C C$ excludes $A x' C$ + $x' C_3$

Summary of 4 letter codes.

Beginning with A, plus some other restrictions.

Sydney's first code — A, no A, no A, no A.

This is

BBB	CBC	DBB		
BBD	CCB	DBD	BBC or DDC	= 16
BCC	CCC	DCC		
BDB	CCD	DDB		
BDD	CDC	DDD	✓ o.k.	

Sydneys second code — A, . . no A, no A

as above, plus A B B / D D = 20

My first code, corrected — A, no C . no A, (nothing with two C's)

A
B D
A C B
D

B B B
D D D

A
B A C
D

A B C / D

BBC or DDC BC B/D = ~~22~~ 24

My second code — A, . . no A, no C

A
B B B
B D D
D

A B
C A D

A B
B C D

[or D C B/D ≡ nothing else B C B/D] = 20 ✓

The 26 Possible sets of the form A, . . .

A ~ C B ~ D

- AAB ABA BAA
- BBB
- AAC ACA CAA CCC
- AAD ADA DAA
- DDD

ABC BCA DCC

ABD BDA

ACB CBA CCD

ADB DBA

ACD CDA CCB

ADC DCA BCC

- CBB CDD
- BBC DDC
- DBB
- BBD
- DDB
- BDD

BAC CAB CDC

BAD DAB

CAD DAC CBC

- BCB DCD
- BDB
- DBD

ABB BBA

ADD DDA

BCD DCB

also for the form

. . . A

Possible codes with A, . . .

No C (where ×)

No A	× × ×	· × ×	× · ×	× × ·	× · ·	· × ·	· · ×	· · ·
× × ×	8	8	9	9	11	11	11	16
· × ×	12	12	16	15	19	17	16	22
× · ×	9	~~12~~	11	12	15	12	~~15~~	18 ?
× × ·	12	15	16	12	16	17	19	
× · ·					20		22	
· × ·					24		20	
· · ×								?
· · ·								

A_1 :

$A_{x\,y\,z}$ A_1

$A_{z\,y\,x}$

Rules for checking words of the form $A, \ldots$

$A \sim C$
$B \sim 1)$

Notation: $A, XYZ,$ $C, xyz.$ and any particular words in: $A, X_0Y_0Z_0,$ $C, x_0y_0z_0,$

for all

Forward rules

$A, AXYZ$ $A, AY_0Z_0A,$

A, X_0AZ_0, A, X

A, X_0Y_0A, A, XY

A, X_0AA, A, XYZ

A, AY_0A, A, XY

A, AAZ_0, A, XY

AY_0Z_0 rejects Y_0Z_0A

X_0AZ_0 rejects Z_0AX

X_0Y_0A rejects AXY

X_0AA rejects AXY and AAX

AY_0A rejects Y_0AA and AXY

AAZ_0 rejects AZ_0A and Z_0AX

Backwards

$YZ, A, CY_0Z_0, A,$

$y\ z\ C\ A$

A, X_0Y_0C, A

$C\ x_0\ y_0\ A$

YZ, A, X_0CZ_0, A

$z\ x_0\ A$

Z, A, X_0CC, A

$z\ C\ x_0\ A\ A\ C$

XYZ, A, CCZ_0, A

$x\ y\ z\ C\ A\ A\ Z_0$

xYZ, A, CCC, A

$xyz, CAAA,$

CY_0Z_0 rejects C_{3y}

X_0CZ_0 rejects x_0Cz

X_0Y_0C rejects y_0x_0C

X_0CC rejects $Ax_0C + x_0Cz$

CY_0C rejects $y_0AC + Cxy$

CCZ_0 rejects $ACz + Czy$

$YZ\ A, CY_0C, A$

$y\ z\ C\ A\ y_0\ A\ C$

CCC -- AAC, $ACz + Cxy$

o.k. ✓

A~C B-D.

26 Sets of the form · A · ·

AAB ABA BAA

BBB

AAC ACA CAA CCC

AAD ADA DAA

DDD

ABC CAB ~~DCC~~ CDC

ABD DAB

ACB BAC DCC

ADB BAD

ACD DAC BCC

ADC CAD ~~B~~CBC

BCA CBA CCD

BDA DBA

CDA DCA CCB

BBC DDC

BBD

DDB

ABB BAB

ADD DAD

DBC BDC

BCB DCD

CBB CDD

BDB

DBB

BDD

DBD

A ~ C B ~ D

26 Sets of the form . . A .

AAB BAA ABA

BBB

AAC CAA ACA CCC

AAD DAA ADA

DDD

—

CAB BCA CCD

DAB BDA

BAC CBA CDC

BAD DBA

DAC CDA CBC

CAD DCA CCB

—

BBC DDC

BCB DCD

BBD

BDB

DBD

DDB

—

ABC ACB DCC

ABD ADB

ACD ADC BCC

CBB CDD

DBB

BDD

—

BAB BBA

DAD DDA

CDB CBD

—