19.1.53

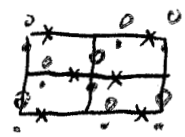
Results of superposition of 3-dimensional Patterson of crystalline Na DNA

Space group C 2

- axes found in superposition function
- mirror planes impossible ∴ asymmetric C

Axial sections

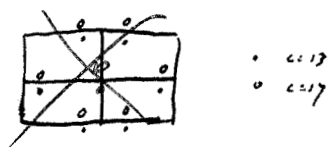
one axial section contains principal maxima (c=0)



the other no important maxima ($c=\frac{1}{2}$)

Peaks at heights 13/30 & 17/30

v strong, also in pseudo-hexagonal array



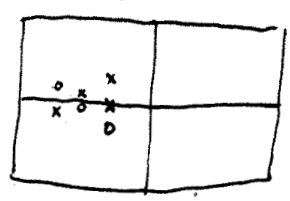
[N.B. hexagons appear canted, ∴ superposition method is not capable of eliminating central peak. But ½ cell reasonable centring w density ½ would have pseudo-cell of side a ~ b ~ 12 Å]

Possible structure having chains along a-c diagonal

but fibres can't be built this way – unreasonable

∴ search for alternative – gives:–

Figure of 8 structure (in projection) } peaks on chain in one cell.



2 pairs of chains / primitive cell (½ pairs / full cell)

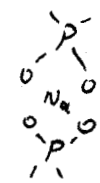
i.e. 56 nucleotides / full cell.

Consistent w density data if

½ ~25% H_2O

½ 2 P atoms per peak

i.e. 2 chains "back to back"



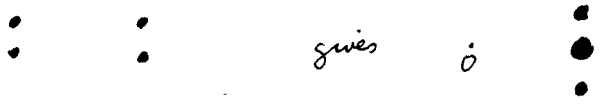
AK

See later, p45, for rejection of this "double helix" with P atoms in fibre period

i.e. chains are ∥ pairs, one upside-down w.r.t the other

Patterson peaks representing Zphosphates

If pairs are all ∥ "orient" & resol" is poor, maxima will give distances between mid-pts of pairs

i.e.  gives

If pairs ⊥ one another, no central overlap

i.e. gives

does this indicate that pairs at c=8 are inclined to other pairs at ½ ∴ give weaker peaks?

Peak at 4·3 Å on section c=2 would then be P-P distance with pair?

but in that case Na is not directly between P-P, or resolution would be destroyed by 2 Na-P peaks

Peak at height 0 lies on axis

∴ 2 P atoms attached to similar nucleotides

- apart from this, symmetry does not control nucleotide sequence except that ∴ a "back-to-back" pair of chains top half of one is similar to bottom half of other

Each chain only) peaks in unit cell

∴ can't reconcile nucleotide sequence with Chargaff's analysis

~~if all chains are same, sequence must be~~ ~~A B C D D C B~~

N.B. Symmetry axis does not affect sequence within one chain

Distance between neighbouring peaks 5.7Å (∴ 3 dimensions)

Nearest to agreement with Chargaff analysis would be

4 purines, 3 pyrimidines, with 2 purines & 2 pyrimidines occupying equivalent positions

- c.f. Broomhead, & similar XRd structures of adenine & guanine

Construction of models

Scale $\frac{1}{2}$" : 1 Å (as for Patterson diagrams)

Backbone chains

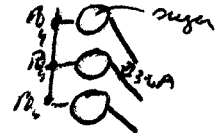
PO_4 tetrahedra – wooden balls, tetrahedrally pierced (France) planes & centres.
Sugar ring constructed (wire) on Furberg model

Coordinate models using only phosphates & sugar rings

show that it is possible to construct straight chain model with P–P = 5·7 Å, all sugar rings & identical pos"n

Pyrimidines for pos" of base chain, are then inclined ~ 25–30° to backbone
- this would leave inter-base plane spacing ~ 5·0 Å

Base-planes can be tilted on this model to give inter-plane spacing 3·4 Å but there is then v little overlap, i.e. v little van der Waals attraction



∴ if P–P distance 5·7 Å, not straight chain

– this (among other things) eliminates a-c diagonal structure

Putting pyrimidine rings ∥ & in full contact we can have 3 phosphates in straight line, & P–P distance ~ 5·7 Å

but 4th must lie well off this line to bring 4th pyrimidine into contact

(system involves some distortion of N_3 bonds)

[linked to sugar]

PTO

If next base is a purine then next P out-of-line could bring 6-ring of purine into contact with pyrimidine

This arrangement for 1 or 3 P has sugar ring nearly || to P chain

⇒ 13 base rings either ⊥ or inclined to chain

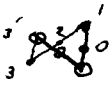
Backbone chain and symmetry at c = 0

Consider 2 pairs of chains 1, 1′ and 2, 2′, separated by $b = \frac{1}{3}$

1 is related to 1′ and 2 to 2′ by diad axis

1 —— 2 and 1′ to 2′ by rotation through 180°

Construct wire model of chain corresponding to Patterson peaks

i.e. 7 steps of each 5.7Å, with 3 successive sets of 3  + reasonable angles

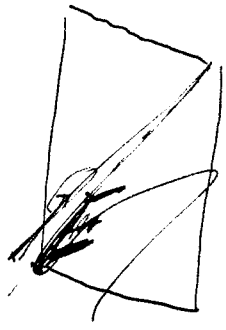
⇒ angle 0–1–2 ~ 100°

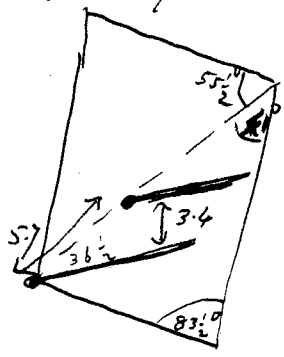
angle 2–3–3′ ~ 110°

For accurate model these angles would be equal, since 3-3′ ∥ 1-0′

∴ angles 100 – 110°

Suppose length of pyrimidine nucleotide is in a-c plane
Then for a-c diagonal peak of structure (i.e. peaks 1'-0-1)



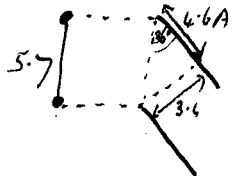


$\sin^{-1}\frac{3.4}{5.7} = 36\frac{1}{2}^\circ$

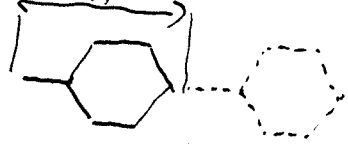
∴ if ~~ba~~ plane of pyrimidine is ⊥ a-c plane, it makes
∠ $36\frac{1}{2}^\circ$ with phosphate chain
and $36\frac{1}{2} + 41 : 77\frac{1}{2}$ with fibre axis

Unlikely the ∠ between base & backbone is so small
- more probable base is also inclined to a-c plane
- this would make its length more nearly ⊥ to both backbone chain and fibre axis

In general, if all P-sugar are equivalent, then $C_1 - C_1' = 5.7$ Å

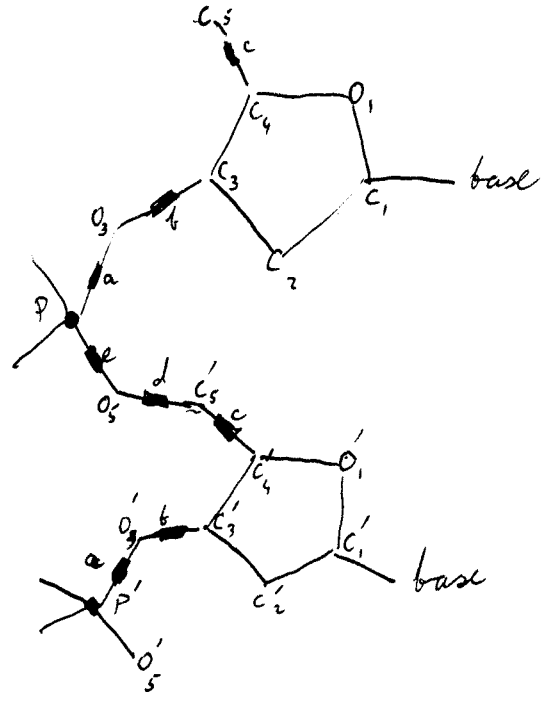


i.e. no overlap of // 4·6Å pyrimidines



∴ sugar rings must be skew to one another,
with ⊥ distance between bonds C_1N and $C_1'N'$ ~ 3·4 Å

- bases then // one another but differently oriented



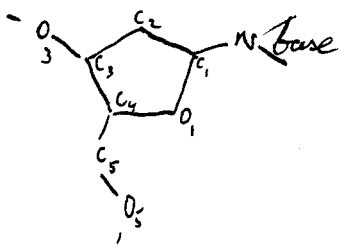
Free rotation of a, b, c, d, e

Wire model of backbone chain and sugar rings

Scale 1" = 1Å

Sugar ring constructed as - Furberg and Beevers + Cochran

i.e. 4 atoms coplanar and C_3' ½Å out of plane, bringing O_3 on to plane



All free rotation obtained by making joints with certain spring ~~[illegible]~~

PO_4 tetrahedra

Requirements

1. Neighboring P on chain 5.7" apart
2. 2 un-bound O of PO_4 facing away from sugar
3. $P\begin{matrix}O\\-O\end{matrix}-$ near vertical plane (Fraser, but this was not for structure A)
4. Possibility of placing neighboring bases parallel at ~ 3.4 Å between planes

Observations

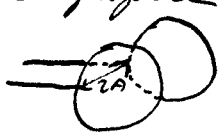
Distance apart of $P\,P'$ determined by rotations b, c, d, eg. c

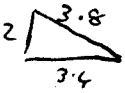
Distance apart of $C_2\,C_5'$ —————— a, b, e

(closest approach ~ 1.2")

Fully extended chain gives $P-P \sim 6.8$ Å

If rdw contact d ~ 3.4 Å between bases, wire spindles are ~ 3Å in diameter and C_1N bonds, seen in projection ⊥ plane of rings, must be > ~ 2Å apart

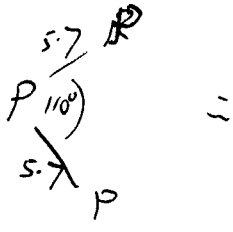




∴ ~~separation~~ distance between N and N' > 3.8 Å

It doesn't seem to be possible to put 3 P groups in a line running 5.7 Å and have C, N bonds in pairs for 11 bases at 3.4 Å separation. Is it possible for 3 P making bend of 110°?

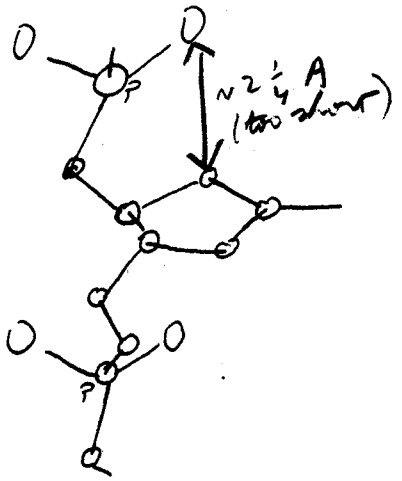
If so, perhaps structure has groups of 2 or 3 bases in contact, and break of contact when chain turns a corner



= this config it is easy to avoid steric hindrance of sugar rings. Not easy for P 5.7 P 5.7 P

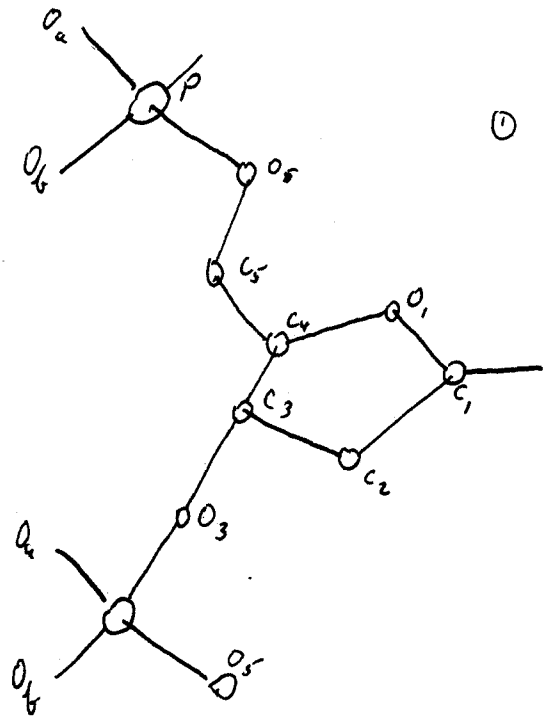
Arrangements of backbone chain with P-P:5'>

1. Sugar rings ~ ⊥ P-P makes it easier to avoid steric hindrance



This leaves $P\langle^{O}_{O^-}$ directed to <u>one side</u> of sugar ring

2. Sugar rings ~ // P-P — again $P\langle^{O}_{O^-}$ to one side



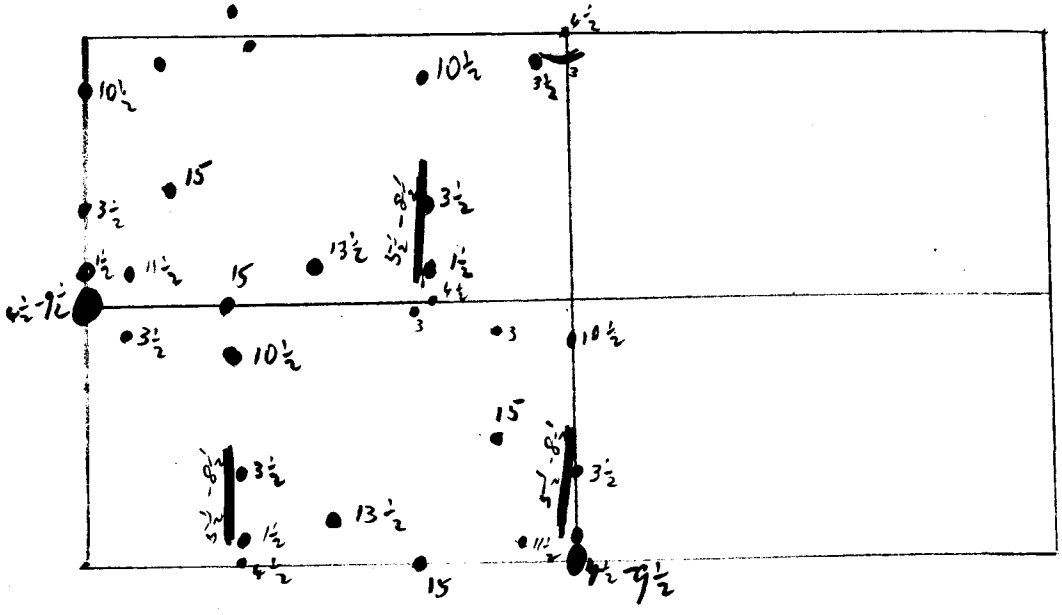
<u>Steric factors</u>

① Make C_5 equidistant from O_3 and O_b

② C_3 tilted away from O_a, but <u>not</u> equidistant betw. O_a and O_5 ∴ this would make C_2 approach $O_{5'}$ ∴ compromise

③ $P-O_{5'}-C_5-C_4$ co-planar
This keeps $O_{5'}$ at max. (& equal) distance from O_1 and C_3

M 9.B



2.2-53

/figure of eight A.K.

Objection to α structure

Part of chain -1, 0 - 1 lies along a - c diagonal

P-P of pair at 0 must lie in a - c plane, ∴

Patterson shows that this must be ∥ along a - c diagonal

i.e. ∥ same direction as chain

∴ impossible

Superposition

To obtain function which gives members of atom-pairs and not their centres, must take account of fact that V_g is not strictly an axial section but on either side of it

Suppose P-P distance in pair = 4.5 Å

and corresponds to peak on section $\frac{3}{4}$ a = 5 cms

the axes at c = $1\frac{1}{2}$, a = $2\frac{1}{2}$ cms

This is M g B

3.2.53

M g B doesn't help solve the problem of how the a - c diagonal streak is related to the $\frac{1}{4}$ - cell heavy peak, nor does it show pos. alternative for for chain

M2g

Peak of height 13 repeats at $\frac{1}{3}$ of away. ∴ this ~~done~~ combining M2 and Mg by placing V_g not at height 0 but at height 13

i.e. put OMg on 0/13 M2, and giving

Mg displacement ÷ 8.3 cms, and M_2 $\frac{1}{2}$ shift where necessary

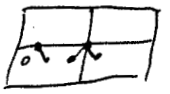
axes are then at height −13 ∠(2.7) ∴ Mg (and a = 0)

∴ draw Mgc derived from MG with axes at height 17

and M2B ∴ ∴ M_2 with axis at 0/17

Principal positions of c:2 vectors : Patterson

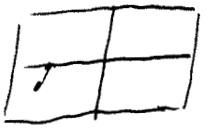
Sections 0 – 2 (twice)



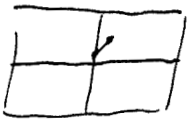
N.B. not at 0

∴ not 11 pairs

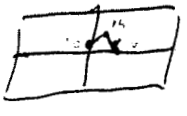
Sections 10 – 12



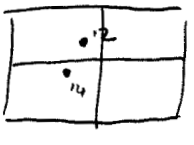
Sections 3 – 5
(or 2 – 4)



Sections 14 – 16



Sections 12 – 14



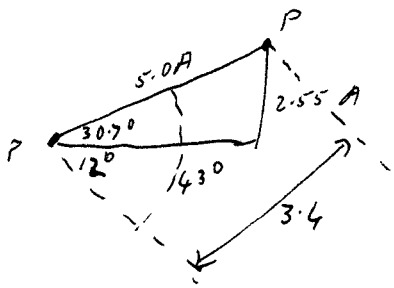
If there are 11 nucleotides per chain

mean inter-P spacing along C-axis is 2.55 Å

If P.P : 5.0 Å

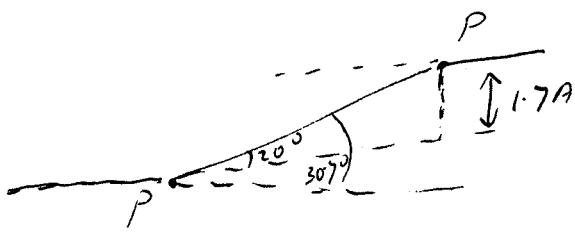
and inter-nucleotide base spacing 3.4 Å

this makes bases inclined at ~ 12° to ⊥ to fibre axis



but then no contact ∴ bases too small

or if chain is ≠



bases inclined ~ 11° to fibre axis

but only 20° to P-P chain

∴ impossible

Possible steps in chain

Predominant near-origin peaks in P are ~ 5Å

① vector 2 peak 122 - strongest of all but c=15
(∴ in general ρ(r))

∴ suppose this is important step in chain

also ② step along a-c diagonal (vector 3

or ③ vector 2, peak 75 (minus of ①, with a-component reversed)

If these are the 3 poss. chain steps, then total number of ②+③ is equal to no. of ①

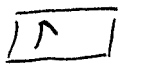
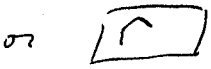
∴ total translation in 'a' = 0

There is no horizontal translation of ~5Å

2 consecutive ① can occur (vectors 2½ ~15)

or 3 " ①

or ① followed by ③ i.e. a possible

but not ① followed by ② but not  or 

N.B. angle of ① in a-b plane is somewhat variable

- probably some peaks lie nearer 'b' axis, to account for resolution power on 'b' axis than 'a' although 'b' axis is further from main maxima

i.e. by

② can be followed by ③ but not by ①

and ③ can be followed by ① (~~surely~~) but not by ②

but ~~③~~ ③ following ① giving peak c~5, b~½ which falls in hole

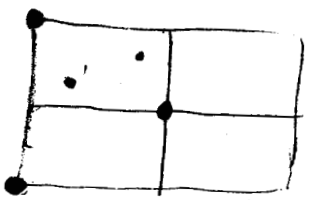
Possible sequences of peaks ① ② or ③

① - ① - ① ② - ② - ② ③ - ③ - ③

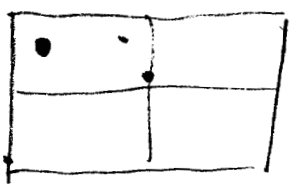
① - ① - ③

M12

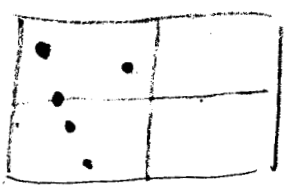
0



1



2



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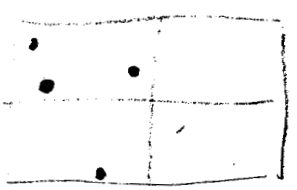


(cont'd from opp.)

This suggests Hooker's work ~~c.a. = 8 days~~

M 11

Peak on section 2, $a = -4.8$ cms $b = 3.3$ cms

Possible pos^{n}s of peaks in -ve region of Patterson marked in, and ~~mark~~ when they coincide with +ve regn of 2nd sheet, they were marked with dotted lines on M 11

M 12

Suppose M 11 vector occurs twice consecutively. Then M 11 is multiple, 2 structures being related by V_{11}

∴ M 12 is M 11 displaced V_{11} on itself

$a = -5\cdot5$ $b = .\cancel{33}\ 3\cdot5$

M 12 Axes on section 7, with a ~ -2.0 cms?

7.2.53

Try M 13, using peak at height 4, a ~ 3.0 cms b = 0 in M 11

distance of this peak from peak on section 1, ?

9.2.53

Possible pos^{n}s of axes in M 11

c = 4	a = 3.5 cms	c = 11	a = -3.5 cms
c = 7	a = -0.5	c = 8	a = +0.5
c = 1	a = -2.5	c = 14	a = +2.5 — no : gives peak on wrong a-c diag. or section 4
c = 4½	a = 0	gives Harker peaks	c = 7 a = 4.8 and c = 11 a = -4.8 } v good

V_{11} gives 2 Harker peaks differing by c = 4, a = 10 cms

∴ superposition of a-c section on itself, with displacement c = 4, a = 10 gives pos^{n}s. Harker peaks & least pos^{n}s. pos^{n}s of axes

10.2.53

Structure B

Evidence for 2-chain (or 1-chain helix) ?

49c - general trend is as for right continuous helix

(which differs from right discontinuous chain in integral no. residues/turn only in contrib^{n} of high order $\bar{J}$'s & the latter)

and this is indistinguishable from double helix with residues on each having same z-value, since 2nd chain has opp. signs in ξ & η terms (eq 1-2), & eq^{n} 2 contains only $R^2 = \xi^2 + \eta^2$ & $\tan\psi = \eta/\xi$

13.3.53.

Axes derived from other possible positions of VII' derived from VII

$\frac{1}{2}(a-5$	$\frac{1}{2}(c+2)$	$a-10$	$c+4$	Harker peaks
-4·7	6	-14·4	14	~~✓~~ ✓
-4·0	6½	-13·0	15	~~✓~~ ✓
7·0	6½	9·0	15	?
4·8	7	4·6	16	?
6·0	3	7·0	8	×
0	3	-5	8	×

Possible pos'n of Harker peaks of V_{11} and axes in M_{11}

Harker peaks are a , c

at a-10 , c+4

then axes is at $\frac{1}{2}(a-5)$ and $\frac{1}{2}(c+2)$

Observed	a - 10 (axes)	c+4	$\frac{1}{2}(a-5)$	$\frac{1}{2}(c+2)$	
V' good (weighted)	1.4	$4\frac{1}{2}$ +	3.2	$(1\frac{1}{4})$ $1\frac{1}{2}$	~~a-5 ; 5 ?~~
no V' X	21.0	$6\frac{1}{2}$ -	13.0	$(2\frac{1}{4})$ 2	
	11.6	$9\frac{1}{2}$ +	8.3	$(3\frac{3}{4})$ 4	IID II axis a = 8.0, c = 4
X	23.0	$10\frac{1}{2}$ -	14.0	$(4\frac{1}{4})$ 4	IIC ~~$4\frac{1}{2}$~~ ? ✓
V' good but axis better @ 6 ✓	12.8	$13\frac{1}{2}$ -	8.9	$(5\frac{3}{4})$ $5\frac{1}{2}$	IIIE ~ no good ∴ origin peaks are lost
V v good	~~26.0~~ 19.8	$13\frac{1}{2}$ +	~~15.5~~	$(5\frac{3}{4})$ 6	
		20	~~14~~ 12.4	9 ✓	II B
		~~5½~~	15.6	$5\frac{1}{2}$ -	

M 9 11

M 9 shows a vector V 11 having one end in common with end of V 9

∴ put M 9 on M 11 with origin at a : 2.4 as b . 6 . 8

and O M 9 11 is O M 9 on 2 9 M 11

i.e. axes on M 11 at a : 2.4 c : 1

if true axes are M 9 axes

M 9 11 like for axes on M 9 axes

M. Wt

~~M~~. primitive unit cell 11.2×10^3

Vol. " " " $12230\ \text{Å}^3$

Suppose partial sp. vol. DNA is 0.55 (as did Riley)

Vol. of 22 nucleotides is $\dfrac{0.55 \times 330 \times 22 \times 10^{24}}{6.03 \times 10^{23}} = 6620\ \text{Å}^3$

$\therefore$ vol. assoc. water $= 12230 - 6620 = 5610\ \text{Å}^3$

$\simeq 45.8\%$ of volume

$\therefore$ Wt % of water is $\dfrac{45.8}{45.8 + 54.2 \times \frac{1}{0.55}} = \dfrac{45.8}{45.8 + 98.7} = \dfrac{45.8}{144.5} = 31\%$

Density of water in Na DNA

Dry density 1.63 gm. vol. .615

Density + 35% (wgt) of water = 1.52 (wgt) i.e. gm. vol. .658

vol. 1.35 g of ~~mixture~~ wet DNA : .889 cc

∴ vol. of .35 g water : .274 cc if vol. DNA is unit.

i.e. density of water : 1.28 g/cc

Suppose density of water : 1.00 g/cm³

Vol of 1.35 g wet Na DNA: .615 + 0.35 = .965 cc

density : $\frac{1.35}{.965}$ = 1.40 g/cc

Suppose density of water 1.00 ~~d~~ of mixture 1.52 i.e. vol 1.35 g : $\frac{1.35}{1.52}$ = 0.89 cc

gm. vol. DNA : 0.89 − 0.35 = 0.54

Suppose partial gm. vol. DNA 0.55

d ——— H_2O 1.00

Then for 40% H_2O, 1.4 g ~~occupies~~ occupies 0.55 + 0.40 : 0.95 cc

$d = \frac{1.4}{.95} = 1.475$

35% H_2O $d = \frac{1.35}{0.90} = 1.50$

30% H_2O $d = \frac{1.30}{0.85} = 1.53$

a - c diagonal

All Patterson peaks streak along forward a - c diagonal

- this suggest possibility of disorder in direction of diagonal

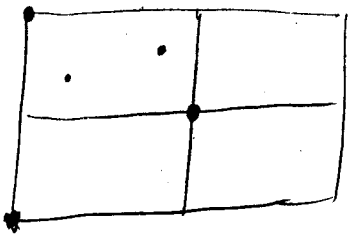
M II C

No good

- Leets 1 – 4 almost nothing

M12 (first 15 sheets only)

0



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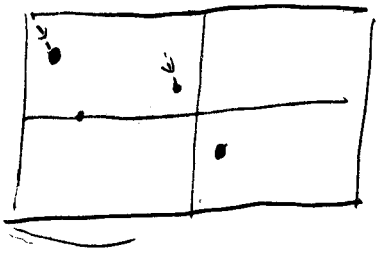

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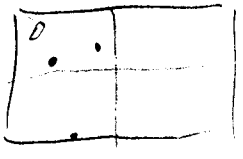

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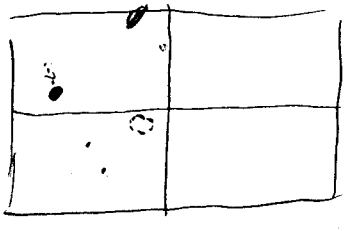

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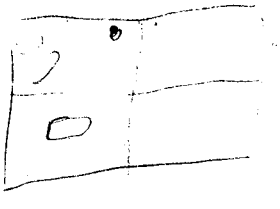

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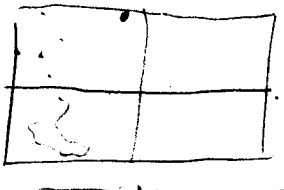

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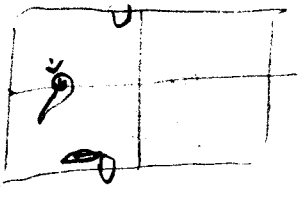

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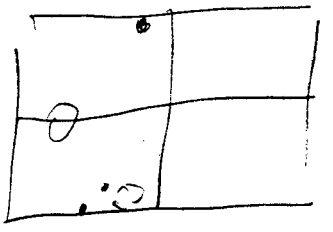

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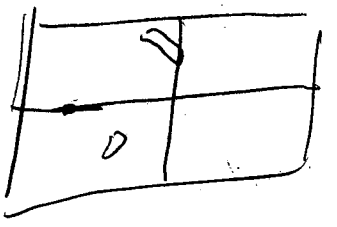

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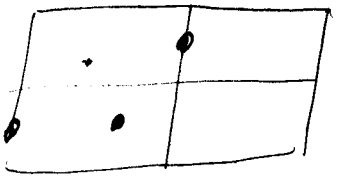

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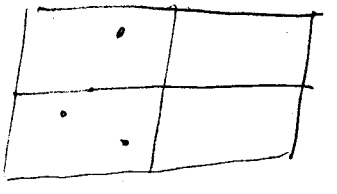

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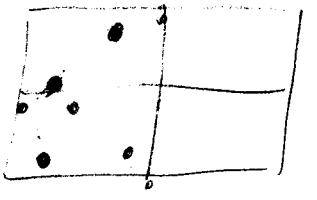

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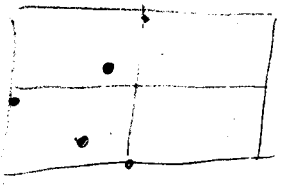

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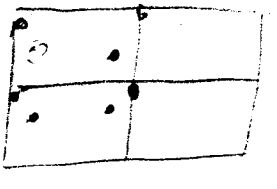

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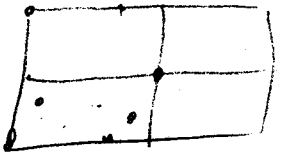
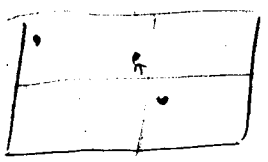


M 4g. 13. 11

O M 13 on 1911, with MB reflected across ~~[illegible]~~ B plane
(i.e. turned over short axis

peaks used are 2 on section 0
and 1 on section 28
(marked with red crosses)

0



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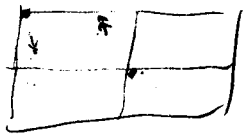

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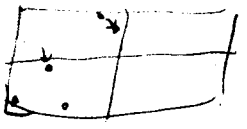

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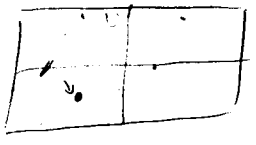

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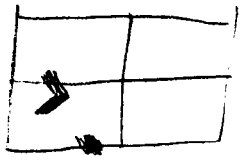


M 13.11

Possible positions of axes

Search for V_{13}', with onset & position. The axis lies ½ way between this and sheet 0

Section 16 — no : 7 & 8 not axial.

Section 13 → bad axial sections

25 "

26 "

5 less bad · axial sects 2/3, 17/18

See preliminary mention of Structure B on 15-2-53 p. 28

23.2.53

Structure B

A.K.

Photograph 51 C

3·4 A are – 158·5 mm on projection

∴ 158·5 = 2R tan 2θ where R is effective specimen-film distance for projection

For $d = 3.40$ A, $\theta_{CuK\alpha} = 13^\circ 4'$ $\tan 2\theta = 0.491$

$$R = \frac{158.5}{2 \times 0.491} = 161.4 \text{ mm} \qquad 2R = 322.8$$

Equator mm	tan 2θ	θ	d (Å)	1/d	λ/d	mm on Bernal chart	Conversion factor
20·2	·0625	1° 48′	24·5	·041	·0629	12·6	(·624)
54·7	·1695	4° 49′	9·16	·109	·168	33·6	·614
82	·254	7° 8′	6·19	·162	·249	50·7	·618
to 100	to ·310	8° 37′	to 5·13	·195	·300	61·7	·617
						mean	·616
120	·372	10° 12′	4·34	·230	·355		
to 152	to ·470	12° 36′	3·52	·284	·438		

These equatorial maxima do not correspond to maxima in $J_0^2(x)$,

which are approximately at 0, a, 2a, 3a

min. $J_0(x)$ for x 3·83 10·18
max. $J_0(x)$ for x 7·02 13·32

Best fit, assume 1st max. is missing (9·16 A reflexion is v weak)

The max. at $\frac{\lambda}{d}$ = ·27, ~~·405~~ ·391, and ·149 ·27

gives $2\pi R r \simeq$ ~~7·24~~ 7·0 for $R = \frac{2\pi\theta}{\lambda} = \frac{1}{d} = \frac{\lambda}{2\pi}$ ~~·1~~ ·175

$\therefore r \simeq \frac{7.0}{2\pi \times 175}$: ~~1·27~~ 6·36

5th layer-line

1st diffuse spot

$2l$: 88 to 100 mm $\tan 2\theta$ .2725 to .310 θ 7°37′ to 8°37′

d: 5.80 to 5.10 $\frac{1}{d^2}$: .0298 to .0385

c^{*2} : $\left(\frac{5}{34}\right)^2$: .02165

$\therefore \left(\frac{\xi}{\lambda}\right)^2$: .0082 to .0169 $\frac{\xi}{\lambda}$: .0905 to .130

ξ : .139 to .200

1st max. for $J_5^2(x)$ has $x \sim 6.5$

$\therefore$ if r : 6.36A, $R = \frac{\xi}{\lambda}$: $\frac{6.5}{2\pi \times 6.36}$: .163

- fits better with max. ~ $J_3(x)^2$

or J_5, $\sim r$: 9.4A, giving $\frac{\xi}{\lambda}$: .113

3rd layer line

1st streak of spots

$2l$: 49 to 65 mm $\tan 2\theta$: .152 to .201 θ : 4°19′ to 5°41′

d: 10.24 to 7.76 $\frac{1}{d^2}$: .00953 to .01665

c^{*2} : $\left(\frac{3}{34}\right)^2$: .00780

$\therefore \left(\frac{\xi}{\lambda}\right)^2$: .00153 to .00885, $\frac{\xi}{\lambda}$: .0391 to .0940

1st max. for $J_3^2(x)$ has $x \sim 4.2$

$\therefore R = \frac{\xi}{\lambda}$: $\frac{4.2}{2\pi \times 6.36}$: .105

for r: 9.4A $R = \frac{\xi}{\lambda}$: .071

but equator, taking r: 9.4A

should have maxima at $\frac{1}{9.4 \times 2\pi}$ (3.83, 7.02, 10.18, 13.32) ~ $\frac{\xi}{\lambda}$

i.e. at .065, .119, .172, .226 ~ zero at 2.40 ~ zero at .0406

or ξ : .100, .183, .265, .348

~ zero at ξ : .0625 i.e. exactly on observed strong peak

2 helices of different radius for simple case of whole number of residues per turn.

Following Cochran Crick & Vand (Acta Cryst. 5 581, 1952)

term $J_n(2\pi R r)e^{in(\psi+\frac{1}{2}\pi)}$ becomes $J_n(2\pi R r)e^{i(n\psi - n\phi + \frac{n}{2}\pi + 2\pi l z/c)}$

(in present case, $l = n$)

For equator $I = \left[J_0(2\pi R r_1) + J_0(2\pi R r_2)\right]^2 = J_0^2(2\pi R r_1) + J_0^2(2\pi R r_2) + 2J_0(2\pi R r_1)J_0(2\pi R r_2)$

For n^{th} layer line, $I = FF^* = J_n^2(2\pi R r_1) + J_n^2(2\pi R r_2) + J_n(2\pi R r_1)J_n(2\pi R r_2)\left(e^{in(\phi - 2\pi z/c)} + e^{-in(\phi - 2\pi z/c)}\right)$

$= J_n^2(2\pi R r_1) + J_n^2(2\pi R r_2) + 2J_n(2\pi R r_1)J_n(2\pi R r_2)\cos\left[n(\phi - 2\pi z/c)\right]$

Here terms in $J_n J_n'$ may give <u>negative contribution to intensity</u>

but on any layer-line, moving out from the meridian, when the first maxim appears in a J_n contribution (i.e. for the J_r term corresponding to largest value of r) there is no negative term in I, since all other J_n terms are small and +ve

∴ even for complex helical structures, first maxima should give maxim diameter.

On equator, first max. (in J_0^2), excluding central max, involves -ve J_0, ∴ max. diameter can't necessarily be got from equator

In general

$$F_n = e^{in(\psi + \frac{\pi}{2})} \left[J_n(x_1) e^{in\alpha_1} + J_n(x_2) e^{in\alpha_2} + \cdots + J_n(x_\rho) e^{in\alpha_\rho} \right]$$

where $\alpha_q = \phi_q - 2\pi z_q / c$

and $x_q = 2\pi R r_q$

and $I = FF^* = \sum_{\rho}^{\rho} J_n^2(x_\rho) + \sum_{\rho \neq q}^{\rho q} J_n(x_\rho) J_n(x_q) \cos[n(\alpha_\rho - \alpha_q)]$

and same argument applies

i.e. first max. give outside radius

but later max. and equatorial non-central max. complicated

2-strand helix with pairs of groups at opp. ends of diameter

$x_1 = x_2$, $\alpha_1 - \alpha_2 = n\pi$

$\therefore$ layer-lines absent for n odd

and $I = 4 J_n^2(x)$ for n even

Conclusion

Structure B does not fit right helical theory, even for low layer-lines. ξ-values of first maxima are too small for right-stranded Helix, & even more so for multi-stranded.

Closing radius of helix so that layer-line maxima fit for right-stranded (i.e. $r = 9.4\,A$) gives a bad fit for equator

Outer layer emanating from 3.4 reflection indicates repeat at 3.4 A is a major — i.e. riser represents structure factor of motif figure, which exists only for $c = n \times 3.4$, & figure repeats for 3.4 A not as for helix

ie J_5 on 5th l.l.
(In R.E.F's terminology, there could still be two chains, unrelated by the symmetry)
See P. 46 A.K.

Structure B if helix is triple-strand helix

nie 2-strand, fitting 5th layer-line max. to $J_{10}(x)$, not require $r \sim 17A$ which is much too big

Suppose ~~diameter~~ radius of outer helix 8·5 A

This gives 3rd layer-line max. at $\xi/\lambda = ~~\cdot 122~~ \cdot 0805$

at 5th ——————— $\xi/\lambda = \cdot 122$

– these values are reasonable, because max $\doteq J_3$ — J_5 is near outer edge of peak

For equator, we then have max. at $\xi/\lambda = \cdot 072, \cdot 132, \cdot 190, \cdot 250$

and 1 zero for $\xi/\lambda = \cdot 045$

– this still has zero rather near the 2~~·5~~ A equator spot

Length of helix of ~~diameter~~ radius 8·5A & pitch 34A

$$l^2 = 34^2 + (8\cdot5 \times 2\pi)^2 = 1156 + 2850 = 4006$$

$$l = 63\cdot3$$

∴ distance between atoms on 8·5A radius helix $= \frac{63\cdot3}{10}$

$= 6\cdot3A$

Intensity of inner $\backslash /$ / $\backslash$ compared with rest of photograph suggests the outer helix ($\sim 8\cdot5A$) is heavy part of structure, i.e. P

For radius 10A

$l^2 = 1156 + 3950 = 5106$ $\quad l = 7\cdot15A$

For radius 9·4A $l^2 = 1156 + 3490 = 4646$ $\quad l = 6\cdot82A$

[1] right-hand helix as above = basis of structure B,
the structure A is probably similar, with P-P distance
along fibre axis < 3.4 A, probably 2-2.5A
(c.f. 2A indicated by pos^{n} of P-P peaks = Pattern
d 2.5A " " 11th layer line reflection)

Many kind a.k.

Single-chain helix for structure B rules out atom-pairings for structure A (with 7 pairs in fibre period)

∴ single chain has 3.4 Å in c between neighbouring P

∴ structure A has less

There is correct a.K.

Suppose important translation in Patterson is

$$c = \frac{1}{11} \quad b = \pm\frac{1}{11} \quad a = -\frac{2}{11}$$ (corresp. approx. to Patterson peak)

Then important reflections are those for which

$$h\left(-\frac{2}{11}\right) + k\left(\pm\frac{1}{11}\right) + l\,\frac{1}{11} = 1$$

$$-2h \pm k + l = 11$$

$$-2h \pm k = 11 - l$$

i.e. on 11th layer-line and expect only 0,0,11

and mass of reflections on layer-lines 6, 7, 8, without (00l) = does not indicate steps of $\sim\frac{1}{7}$ in c

These reflections due to the bases. R.E.F. missed this. AK.

Structure B

7th layer-line

$2l$: 122 – 138 mm to 2θ : 378 to 427

θ : 10° 21′ to 11° 34′ d : 4·28 to 3·84 A

$\frac{1}{d^2}$: ·0546 to ·0678

$\left(\frac{m}{c}s^2\right)$: $\left(\frac{7}{64}\right)^2$: ·0424 ∴ $\left(\xi/\lambda\right)^2$: ·0122 to ·0254

ξ/λ : ·110 to ·159

I.e. max. for $J_7(x)$ has $x \sim 9.0$

∴ for $r = 8.5$,

$R = \xi/\lambda = \frac{9}{2\pi \times 8.5}$: ·168

for r : 9·4 ξ/λ : ·152

N.B. Here we expect observed max. to be displaced inwards : Lorentz etc

7th layer-line should also have max. of same value as 3rd

i.e. ξ/λ : ·039 to ·094

– this is apparently absent

3-chain ~ 2-chain helix?

Chains are not equally spaced, ∴ this would mean n^{th} layer-line contains $\frac{7}{3}n$'s

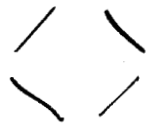
∴ 3-chain helix is highly improbable

∴ chains would be non-equivalent (2 chains ~~change~~ would be equivalent)

Also ∵ structure A believed to have 2 chains / unit cell

R.E.F. is not (as) making the correct connection between the A and B. A.K.

N. B.

Outer Patter  emanating from 3·4 spot is not equator

of patter from origin. if it were this would

cross on 5th layer-line

Inner meets on 5th layer-line

$J_{10}(x)$ has first max. for $x \sim 11.8 = 2\pi R r$

Observed max. on equator, $R = .162$ & $.195$

$\therefore r = 11.6$ & 9.6

Here observed max. is displaced inwards $\therefore$ 3rd max. of J_0 for $r = 9.4$A has $R = .172$

Density

Volume of cylinder radius 10A, height 34 A $= \pi \times 100 \times 34 = \frac{10700}{\cancel{11400}}$ A^3

Vol. dry nucleotide (density 1·63) = 336 A^3

$\therefore$ no. nucleotides / cylinder $= \frac{10700}{336} = 32$

Since some fairly dry fibres give structure A, density of cylinder is prob. near density of dry Na DNA, water lying mainly outside cylinder.

$\therefore$ this suggests 3 chains

but not easy to reconcile w structure A

For helix of radius 8·5A Vol. cylinder $= \pi \times 8.5^2 \times 34 \simeq 7700$ A^3

no. nucleotides $= \frac{7700}{336} = 23$

A form
Superposition map

5. 3. 53

M 11

Uses peaks on section 2 units, it seems, must be a P-P peak. Other superpositions may be fruitless : used part of Patterson not due to P-P

V 11 is clearly multiple — or, more probably, peak is due to agglomeration of near-equal vectors. ∴ should be several valid positions for axes (as described q. 2. 53)

∴ take M11B and M11D and look for possible chain common to each — allowing shift & b-direction of one relative to other

To find correct pos^n of M11B w.r.t M11D, look for the 4 origin peaks in each

— these are at height 8 — 11 D in M11B — & 3, 5 in M11D

(M11C no good, as shown by fact that origin peaks are lost)

M11B can be put on M11D in 4 ways

1/ axes of 0 on 11B may correspond height 15 on 11D

∴ ~~rotate through 180° and~~ put 0-7 on 15-8

i.e. on 15-8 upside-down

2/ 11B and 11D may give different enantiomorphs

— this corresponds to 0-7 — 0-7 rotated and upside-down

i.e. poss^n's are
i) 0-7 on 0-7
ii) 0-7 — 0-7 rotated and upside-down
iii) 0-7 on 15-8 upside-down
iv) 0-7 — 15-8 rotated

M11D 0-7 on M11B15-8 upside-down

11D 0-7 at ~~~ ~~~ ~~~

Presumably during the [illegible] REF was
[illegible] no. ~~[illegible]~~ on the B form. "Rough draft"
dated 17 March 1953

M11 superpositions 18.3.53

~~M11 B and M11 E both have origin peaks of height 8 & 10~~
~~These have different 'a' values, ∴ must relate to different chains~~

~~How can M11 E, 8-15 be fitted to M11 B?~~

M11 B has origin peaks at 8 & 10, M11 E at 5, 7
These have different 'a' values, ∴ either belong to diff. chains
or to diff parts of same chain

A. Diff. chains, same heights

~~M11 E 0-7 on M11 B 8-15 upside-down~~

a: 0 b: +7.9 cms
general fit on other peaks less good

M11 E 0-7 on M11 B 8-15 rotated

a: b/2, b: 11.8 cms good on both sets

M11 E 0-7 on M11 B 0-7

a: 1/2 b: −1.0 cms

a: 0 b: −8.2 cms ~~origin~~ 0 peaks good
a: 0 b: +8.8

M11 E 0-7 on M11 B 0-7 rotated and upside-down

Is structure A triclinic?

2-axis can't pass through DNA chain : asymmetric sequence

but superpositions always show peak on axes

If peaks are P, axis can only be pseudo-axis

i.e. array of P monoclinic, but true symmetry triclinic

In this case, whole Patterson is wrong

- each reflection is unresolved pair, (hkl) and $h\bar{k}l$)

[If structure is triclinic of P's monoclinic will Patterson give correct P-P vectors?]

If structure truly monoclinic

either chains don't go through axes

i.e. no peaks on axes

or sequence of phospho-ester links is 3 3 5 5 3 3 .. etc

- this is symmetric about phosphorus atoms

but unlikely a) : evidence for enzymatic degradation

b) : prob. unless ~~A~~ get ~~5A~~ equally spaced bases, distance > 3.4Å

21. 4. 53

Intensities of structure A suggest equally spaced chains (pseudo-halving of cell)

Then unit has true diad $\frac{1}{2}$-way between planes

+ pseudo-diad through chain, relating phosphates only

- can we arrange units so that pseudo-diad applies to whole structure and true diad does not?

Pseudo-diad passing through P is only possible if chains are equally spaced.

Vertical distance between 2 chains would then be ~ same as shorter vertical distance in Crick model.

Shapes of Patterson peaks

All peaks are stretched along a.c axis

- can this be due to P···Na ≈ that direction ?

- well-resolved ~~beak~~ peak on C:2 suggests that Na does not lie half-way between 2 P's

Shapes of P-P, Na-Na, and P-Na peaks were calculated by approximating f^2 curve (or f_P, f_{Na}) by $e^{-a^2 s^2}$ and taking account of artificial temperature factor used

Results

P-P	r(Å)	0	0.5	1.0	1.5	2.0	2.5	3.0
P-P	P(r)	115.2	108.0	88.8	64.0	40.4	22.6	10.9
Na-Na		66.3	59.4	42.6	24.1	11.4	4.3	1.3
P-Na		85.2	78.5	61.8	41.3	23.5	11.4	4.7
P-P + Na-Na		181.5	167.4	131.4	88.1	51.8	26.9	12.2
2 (P-Na)		170.4	157.0	123.6	82.6	47.0	22.8	9.4
Shape of peak for P-Na distance 3.0Å		190.9	190.2	178.4	170.7	175.4	183.9	182.6
Shape of peak for P-Na 2.5Å		204.3	214.4	213.0	211.7	208.8	197.3	169.2
Shape of peak for P-Na 2.0Å		228.5	250.0	255.0	245.1	222.2	183.9	135.8

Isolated Patterson peaks mostly have max. dimension approx. twice min. dimension

$\frac{1}{2}$-peak width of P-P + Na-Na (Patterson) $\sim 1.5 \times 2$ Å

$\therefore$ this is minim dimension.

$\therefore$ Å $\frac{1}{2}$-peak width of P—Na combination must be $\sim 3.0 \times 2$ Å

$\therefore$ this requires P - Na distance ~ 2.0 Å

7.5.53

Attempts to adapt Watson and Crick model to structure A

Modifications introduced

1/ P–P distance decreased from 7·0 A to 5·3 A
(as suggested by peaks on sections 2-3)

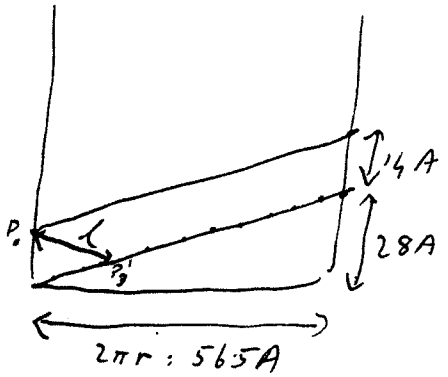
2/ 11 nucleotides per turn instead of 10
(as suggested by meridional peak on 11th layer-line)

3/ 2 chains of helix are equally spaced
(as suggested by pseudo-halving of cell
& indication on Patterson that only part of structure
repeats at half-cell height

4/ P on radius 9A instead of 10A
(as indicated by cylindrical Patterson)

Suppose chains equally spaced
and P's vertically above one another in chain

Draw schematically un-wrapped helix



Suppose P_0 P_3' are linked through
atom C_3' of same purine-pyrimidine
complex. Then on W & C model
$P_0 - P_3' = 15·2A$

To obtain length of arc on un-wrapped helix, consider helix of
same radius, of which P_3' P_0 are is a part
Then this helix makes 3/11 of a turn ∴ height $\left(\frac{1}{2} - \frac{3}{11}\right) \times 28A = \frac{5}{22} \times 28A$
i.e. whole turn ∴ height $\frac{5}{22} \times \frac{11}{3} \times 28 = \frac{5}{6} \times 28 = 23·4A$
∴ length of whole turn $= \sqrt{56·5^2 + 23·4^2} = \sqrt{3192 + 548} = \sqrt{3740} = 61·2A$
∴ length of arc $l = \frac{3}{11} \times 61·2 = 16·8A$

8.5.53

Length of P-P' bracket through C_3's to same P_4-P_5 complex

Crick says 15.2 Å

but this is inconsistent w other data of his model - too small

$C_1 - C_1' = 11$Å

$C_1 - P \sim 3.5$ Å (from wire model)

and these are fairly nearly co-linear

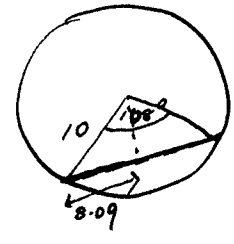
$\therefore PP' \sim 18$Å

this is consistent with other W & C data

When chain contracts & form structure A, $P - C_3$ can't decrease much - contraction must occur between C_3 & P on other side

$\therefore PP'$ still ~ 18 Å

If $P_0 P_0'$ are vertically above one another, distance 15 Å



x-y sep of $P_0 P_3'$ is 16.18

z sep $(15.0 - 3 \times 3.4) = 4.8$ Å

$\therefore P_0 P_3' = \sqrt{16.18^2 + 4.8^2} = \sqrt{261.8 + 23.0} = 16.8$ Å

If P_0 rotated ~ 1 Å behind P_0' on helix

$P_0 P_3' \sim 17.6$ Å

11-residue helix : structure A

Difficulties

Can they have one helix / primitive cell

∴ how account for 13 Å vector ⊥ C plane?

↳ how account for pseudo-trans

Density

Vol. dry nucleotide, density 1·63 g/cc, = 336 A^3

Partial sp. vol. 0·55 (Kahler, J. Phys. Coll. Chem. 52 1948 676)

Suppose partial sp. vol. in structure A is 0·55

In 330 g occupy $0.55 \times 330 = 181.5$ cc

1 nucleotide occupies $\frac{181.5 \times 10^{24}}{6.03 \times 10^{23}}$ $Å^3$ $= 296$ $Å^3$

1 molecule H_2O occupies $\frac{18 \times 10^{24}}{6.03 \times 10^{23}} = 29.85$ $Å^3$

Vol. of complete unit cell 2450 $Å^3$

1 nucleotide + 4 H_2O	415 $Å^3$	giving 59 nucleotides / unit cell
" 5 "	445	55
6	475	51·5
7	505	48·5
8	535	45·7
9	565	43·3

Structure B. Suppose 24·5A reflection is (100) of hexag. close-packed rods

Then vol. unit cell: $\frac{2}{\sqrt{3}} \times 24.5^2 = 694$ $Å^3$ $\times 34 = 694 \times 34$ $Å^3$

Suppose this contains 20 nucleotides, i.e. M.Wt $20 \times 330 = 6600$

then density due to nucleotides only is

$$\frac{6600}{6.03 \times 10^{23} \times 694 \times 10^{-24} \times 34} = 0.465 \text{ g/cc}$$

∴ if true density is 1·52 g/cc

water content must be $\frac{1.52 - 0.465}{0.465} \times 100 = 227\%$ of dry weight!

If 40 nucleotides = unit cell

water content is $\frac{1.52 - 0.93}{0.93} = 63.5\%$ of dry weight

still high, but more reasonable

11. 5. 53

Equatorial reflections in structure B

Main reflection ~ 24·5 Å

If this is inter-helical distance, density is much too low

Some inter-penetration of helices in one direction must be possible, the spacing in other direction being 24·5 Å

but nucleo-protein gives same spacing, 24·5 Å,

and in this case, on W & C model, inter-penetration quite impossible

spacing measured on R & W's published photos

Distances in Å

	① R & W	② Structure B	Ratio ①/②
equatorial	15·4	7·5	2·05
2nd equatorial	21·7	10·3	2·1
3·4 Å reflection	111	57	1·95

Density calculations (see above) suggest packing is such that there are 2 helices per unit cell

(i.e. not hexag. close-packing

- reasonable ∵ helix hasn't got hexag. symmetry

M. Wt. of 20 nucleotides 6600

+50% H_2O 9900

∴ X-section of unit cell, for density 1.50 is

$$\frac{9900 \times 10^{16}}{6.03 \times 10^{23} \times 1.50 \times 34 \times 10^{-8}} \text{ Å}^2 = 322 \text{ Å}^2$$

If hexag. close-packing, $\frac{\sqrt{3}}{2} a^2 = 322$ $a^2 = 372$

$a = 19.3$

If distorted, $a\,b \sin\gamma = 322$

and $b \sin\gamma = 24.5$ (∵ strong reflection)

∴ $a = 13.1$ Å - impossible for W & C model

or Unit cell contains 2 helices

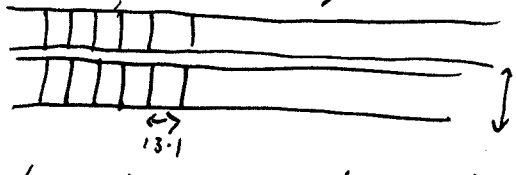
and $a = 26.2$ Å.

This is only slightly distorted from graphite-like structure,

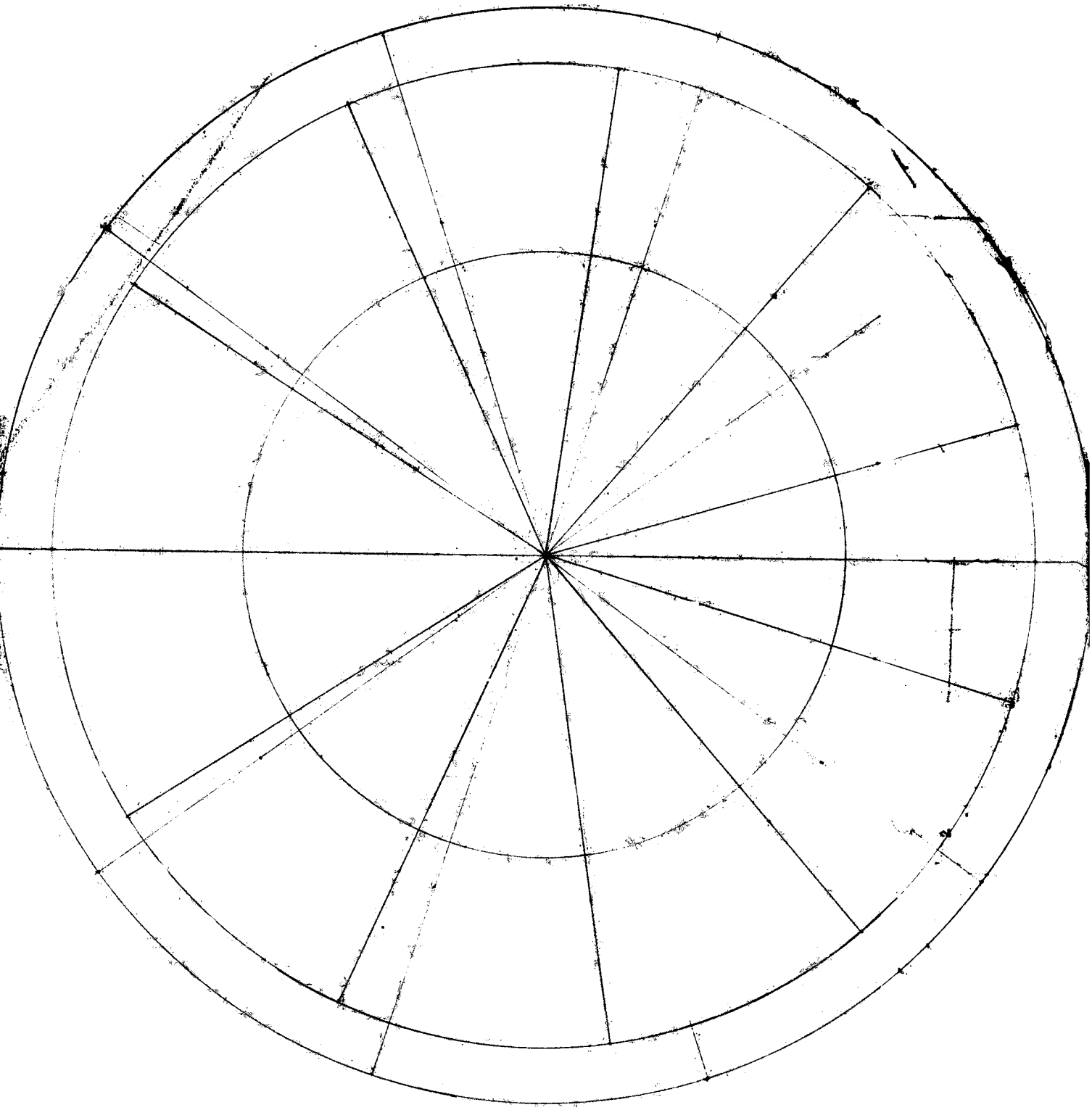
giving inter-helical distance ~ 16 Å

∴ Helices in sheets, with inter-sheet sep^n 24.5 Å and inter-penetrating

giving other dimension $\frac{322}{24.5} = 13.1$ Å



In nucleo-protein, then 13.1 Å must have to expand, and 24.5 Å stays const.



1cm = 1Å

W & C modified for structure A

Cylindrical Patterson ~~[illegible]~~ suggests helix of diameter 18A

∴ suppose P_1' on helix of radius 9·0A

and 11 residues per chain (∵ 11th layer-line reflection)

Horizontal spt of P-P on 10A, 10-residue helix : $20 \sin 18° = 6.18$A

9A 11-residue helix : $18 \sin \frac{32.23°}{2} = 5.07$A

P-P for B : $\sqrt{6.18^2 + 3.4^2} = \sqrt{38.19 + 11.56} = \sqrt{49.65} = 7.05$A

A : $\sqrt{5.07^2 + 2.55^2} = \sqrt{25.70 + 6.53} = \sqrt{32.23} = 5.68$A

∵ near inter-base distance is const. ∠ of tilt ~40°.

Suppose ∠ of tilt 40° and $C_1' - C_1'$ const. at 11 Å

then horiz. spt of $C_1' - C_1' = 11 \cos 40° = 8.4$A

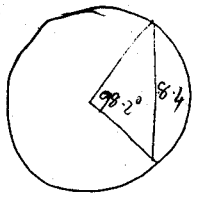
~~∴ C_1' lies on ⊙ of radius 4·2A~~

Suppose P_n and P_n' lie vertically above one another

(∵ 2-height peak suggests this ∴ approx. true)

Then on ⊙ containing all C_1', ~~then~~ chord subtending $\frac{3 \times 360°}{11}$

at centre is of length 8·4A



radius : $\frac{4.2}{\sin 49.1°} = 5.55$A $\frac{4.29}{\sin 49.1} : 5.67$A

[for structure B, equivalent radius is $\frac{5.5}{\sin 54°} = 6.8$A

∴ radial extension of sugar + phosphate ~ same in both cases]

Horizontal spt of $C_1' - C_1'$ is then $5.55 \times 2 \sin \frac{360}{2 \times 11} = 3.12$A

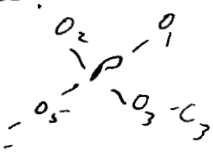
Total $C_1' - C_1'$: $\sqrt{3.12^2 + 2.55^2} = \sqrt{9.73 + 6.53} = \sqrt{16.26} = 4.03$A

Model giving approx right distances & reasonable angles

C_2 equidistant from O_1, O_5-

~~P - O_3 - C_3 - C_2 coplanar, ~ in vertical plane.~~

~~Also coplanar with O~~



giving max. & min distances for C_2O_2 & C_2O_5

~ planar

P - O_5 - C_5 - C_4

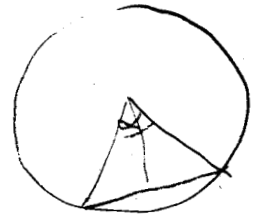
P - P 5.7 Å $C_1' - C_1'$ 4.04°

$C_1'N$ points ~ 40° upwards (when $O_3 - C_3$ is below P)

Helix of radius 9.0 ~~Å~~ Pitch 28.1 Å

Length of one turn $= \sqrt{(2\times 9\pi)^2 + 28.1^2} = \sqrt{56.55^2 + 28.1^2} = \sqrt{3198 + 790}$

$= \sqrt{3988} = 63.15$ Å



$\alpha = \frac{360}{11} \times n$

x-ept of vector on cylindrical Patterson

$= 2 \times 9 \sin \frac{360 \times n}{11 \times 2} = 18 \sin 16.35\, n$

$x_1 = 18 \times .2815 = 5.07$

$x_2 = 18 \times .5407 = 9.74$

$x_3 = 18 \times .7559 = 13.60$

$x_4 = 18 \times .9098 = 16.37$

$x_5 = 18 \times .9858 = 17.80$

Distances of atoms from axis i projection

with base tilt 4 0°

① r	② 2πr	③ 2πr × ·088	$J_0(3)$
0·78	4·9	0·43	·95
1·31	8·2	0·72	·87
1·88	11·8	1·04	·75
2·28	14·3	1·26	·65
2·63	16·5	1·45	·55
2·73	17·2	1·51	·51
2·88	18·1	1·59	·46
3·06	19·2	1·69	·40
3·11	19·5	1·72	·39
(½)3·35	21·0	1·85	(·31)·16
3·86	24·3	2·14	·14·
3·92	24·6	2·16	·13
4·09	25·7	2·26	·08
4·10	25·8	2·27	·07
6·12	25·8	2·27	·07
4·44	27·9	2·45	·02
4·54	28·5	2·51	$\cdot\overline{05}$
4·55	28·6	2·51	$\cdot\overline{05}$
(½)4·90	30·8	2·71	$(\cdot\overline{15})\cdot\overline{08}$
5·10	32·1	2·82	$\cdot\overline{19}$
5·67	35·6	3·13	~~·20~~ $\cdot\overline{21}$
5·67	35·6	3·13	$\cdot\overline{21}$

Total 21

Intensities in structure A

If one helix per lattice point then, ~~equatorial~~ intensities depend only on structure factor of helix

∴ can't explain large diff. I for (130) and (200)

is this wrong, → large error in Patterson?

To calculate equatorial intensities, only require radial distance of each atom.

Suppose base complex tilted 40°.

Drawing (1" : 1Å) gives $C_1' - C_1' = 11.2$ Å

∴ (see 2 pages back) these lie on helix of radius 5.67 Å

Suppose tilt is about "diad" of complex. Then draw foreshortened complex by reducing distance of each atom from diad by factor ~~cos~~ cos 40° = 0.766. This gives projection

Then measure distance of each atom from axis

Intensities & positions of 1st equatorial reflection

Continuous transition from ~17 Å in near-dry DNA through 19 Å for structure A → >24 Å

This suggests that reflection has same significance in 2 phases
i.e. related to inter-unit distance in both cases

Intensity appears to have min. at ~19 Å

- c/ dry rather dry photo 34 in which reflect ~17–18 Å is stronger than round 19 Å in structure A

[Dry photo 34 has meridional arc of larger spacing than structure B (d ~ 36 Å) ?]

Spacing on photos showing A+B (e.g. 75, 5,) ~ 20 Å + intensity lift

52 & 53 are same specimen as 51, at higher RH (92%)
- they have same equatorial spacing

Tilt of bases in structure A

6, 7, and 8 layer-lines suggest $\sim 25°$

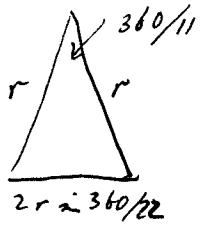
$\therefore$ ~~3~~ 5/3 mean values are 0·56, 0·48, ·44 for these layer-lines

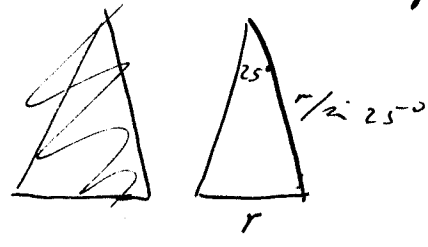
i.e. $\tan^{-1}$ 29°, 26°, 24°

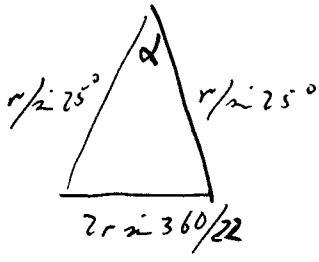
Suppose tilt 25°, find ∠ between planes of neighbouring bases

i.e. ∠ between ⊥'s to planes of bases

These lie on cone of semi-vertical angle 25°





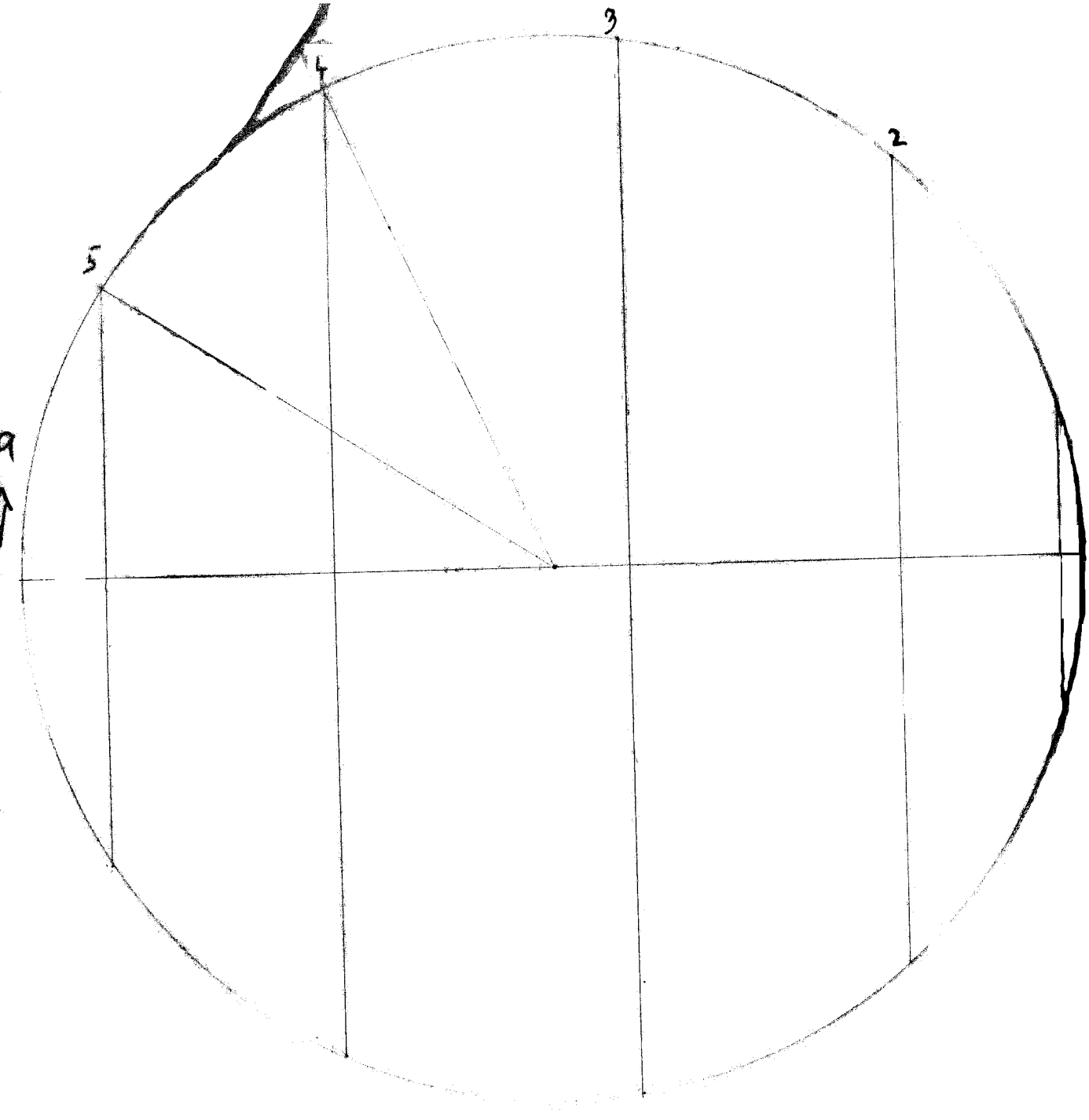


$$\alpha = 2\sin^{-1}\left(\sin\tfrac{360}{22}\sin 25\right)$$

$$= 2\sin^{-1}\cdot 2818 \times \cdot 4226 = 2\sin^{-1}\cdot 11.9$$

$$= 2 \times 6°\,50'$$

$$\simeq 13\tfrac{1}{2}°$$


3
4
2
5

Harker peaks for helix of radius 9A (structure A)

	'a'		δ = $\frac{1a'}{22} \times 254$	Å	
1.	$18 \sin \frac{360}{22}$	$= 18 \sin 16.36° : 18 \times .2818 : 5.07$	$\frac{c}{11}$	0.6	3.2, 17.2
2.	$18 \sin 360 \times \frac{3}{22}$	$: 18 \sin 49.1° : 18 \times .7559 : 13.6$	$\frac{3c}{11}$	1.6	9.3, 23.2
3.	$18 \sin 360 \times \frac{5}{22}$	$: 18 \sin 81.85° : 18 \times .9899 : 17.8$	$\frac{5c}{11}$	2.1	14.9, 0.8
4.	$18 \sin 360 \times \frac{2}{11}$	$: 18 \sin 65.5° : 18 \times .9100 : 16.4$	$\frac{7c}{11}$	1.9	19.8, 5.8
5.	$18 \sin 360 \times \frac{1}{11}$	$: 18 \sin 32.72° : 18 \times .5404 : 9.74$	$\frac{9c}{11}$	1.2	24.2, 10.1

δ is : a-b sections are not ⊥ to fibre axis.

± δ depending on orientation (or hand) of helix

Examination of intra-helical vectors on 3-dimensional chains orientated to hand to be as indicated opposite, & this gives + δ

Suppose the 2 helices on which P atoms lie are related by vector V_1

and suppose a vector v on Patterson is a P – X interaction, where X is any atom ~~other than P~~ (e.g. N_a)

then there is a similar vector $V_1 - v$

Suppose V_1 has $x = -1$ Å
$y = 0$
$z = 13$ Å (= section 14)

then find which Patterson peaks, un-accounted for by P-P vectors, occur in pairs v and $V_1 - v$. These will be P – X vectors

e.g. ~~xyz~~ v ~~section 10, $x = 6$ Å $y = 0$~~
$V_1 - v$ ~~section 4~~

v section 12 $x \sim 8$ Å, $y \sim 7$ Å
gives section 2 $x \sim -9$ Å $y \sim -7$